# Modeling Energy-Related CO<sub>2</sub> Emissions with Backpropagation and Metaheuristics

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Abstract—In this paper, we propose a model that combines Backpropagation Neural Network (BPNN) with a metaheuristic algorithm to predict carbon dioxide (CO<sub>2</sub>) emissions. The model utilizes input variables directly influencing carbon dioxide emissions. Our objective is to monitor CO<sub>2</sub> emissions based on energy consumption resulting from production processes driven by the corresponding energy demand. Model training and testing are conducted to identify the most suitable model. The results demonstrate that machine learning with the Particle Swarm Optimization (PSO) model achieves an optimal avoidance rate. To assess model accuracy using Mean Square Error (MSE) and Mean Absolute Error (MAE) the smallest error indicates a more precise prediction. Following established guidelines, this document aids managers in making informed business decisions and devising energy management policies that effectively monitor carbon emissions.

Keywords— CO<sub>2</sub> Emissions Prediction, Backpropagation Neural Network, Metaheuristic Algorithms, Particle Swarm Optimization

# I. INTRODUCTION

Global warming refers to the phenomenon in which the Earth's average temperature increases due to the greenhouse effect, a well-known process characterized by the accumulation of greenhouse gases [1]. This effect is primarily attribute to human activities, specifically the release of carbon dioxide (CO<sub>2</sub>) resulting from the combustion of various fuels in energy consumption processes. Key factors contributing to global warming include the heightened emissions of pollutants, resulting in increased permeability of the atmosphere to solar radiation. This phenomenon is known as the greenhouse gas effect.

The critical greenhouse gases that require reduction include carbon dioxide (CO<sub>2</sub>), and the escalation of CO<sub>2</sub> emissions is related to final energy consumption from various sources such as coal and coal products, crude oil and petroleum products, gas, and electricity. The challenges posed by global warming have prompted countries to address the management of energy needs and the reduction of greenhouse gas emissions. Accurate predictions of energy requirements and CO<sub>2</sub> emissions are crucial for effectively addressing the challenges and planning energy management strategies.

The application scope of machine learning is extensive, with neural networks emerging as a widely embraced technique for predictive modeling, particularly in scenarios demanding high prediction accuracy, such as medical data and scientific research. Neural Networks offer an alternative approach to predictive modeling, extensively employed in various forecasting tasks. Among these, the Multi-Layer Perceptron (MLP), a prevalent type of Neural Network (NN), Tidarat Luangrungruang\* Department of Computer Faculty of Science and Technology Sakon Nakhon Rajabhat University Sakon Nahon, Thailand tidarat@snru.ac.th

has found widespread application across diverse practical challenges. Neural networks exhibit superior learning capabilities from unstructured data compared to other methods, owing to their distinct learning architecture, differing from general machine learning algorithms. However, training MLPs for specific applications presents challenges, often grappling with issues concerning local optima, overfitting problem, encompassing convergence rate, training speed, and sensitivity to initialization. Numerous studies have demonstrated the efficacy of several methods in predicting carbon dioxide emissions [2][3][4][5][6][7][8]. This article aims to address these challenges by employing five metaheuristic algorithms to train MLPs, specifically focusing on predicting carbon dioxide emissions in Thailand.

# II. BACKPROPAGATION ALGORITHM

The supervised learning model is extensively used in machine learning, wherein a model undergoes training on a dataset. The Multi-Layer Perceptron (MLP) represents a neural network of higher complexity compared to a single perceptron, featuring interconnected hidden layers that form a mathematical model simulating the relationship between data and desired outcomes [9]. MLP offers various advantages such as classification, prediction, and problem-solving capabilities. In this approach, neurons within the hidden layer adjust their weights based on computed results, typically initialized randomly. Another notable learning model is reinforcement learning, which involves multiple layers and employs a feed-forward connectivity system. When dealing with multiple layers and a feed-forward connectivity system, the process is termed the backpropagation (BP) algorithm [10]. This learning mechanism entails transmitting error information during result computation, facilitating the adjustment of weights between layers to optimize computational efficiency [11][12][13].

## **III. METAHEURISTIC ALGORITHM**

Metaheuristics are applied to enhance performance in modified and adaptable problem domains [14]. They provide significant benefits when handling large-scale problems that are impractical for exhaustive analysis or comprehensive surveying. Employing metaheuristics addresses and enhances solutions for diverse optimization problems, considering challenges stemming from incomplete or limited data and computational resources. Metaheuristics encompass a range of algorithms that aim to efficiently explore solution spaces, aiming for near-optimal or optimal solutions without exhaustively evaluating all possible solutions. Metaheuristics algorithm often involve iterative processes that explore different parts of the solution space, balancing exploration and exploitation to efficiently converge on good solutions [15][16][17].

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## A. Biogeography-based optimization (BBO)

BBO is an evolutionary metaheuristic inspired by the dispersal behavior of living organisms across various islands [18]. Frequently, populations migrate from islands with high fertility to those with lower fertility, resulting in increased fertility on the settled island due to the introduction of a diverse set of species. In this analogy, islands can represent solutions to a balancing problem, where suboptimal solutions are more likely to adopt characteristics from others, particularly better solutions. While existing good solutions are less prone to acquiring traits from other solutions, they are expected to evolve and develop into even better solutions over time. Overall, the BBO algorithm capitalizes on this idea of emulating the natural dispersal and adaptation observed in living organisms across different environments, leveraging the concept of migration between islands to optimize and improve solutions in problem-solving scenarios [19][20][21].

### B. Jaya Optimization (JAYA)

The Java Algorithm was devised to tackle extensive variable optimization challenges without specific targeting, conditions, or preset parameters [22]. It operates through a simulated natural population dynamics concept, randomly adjusting population variables to enhance suitability. These adaptations encompass the entire population, selecting variables to improve the target function and subsequently adjusting variables in the next generation. Its proficiency lies in resolving various constraint problems without complex parameter modification. Functioning as an inhibition-free search algorithm, it adeptly handles numerous parameters or computationally intense methods. Distinguished from other algorithms, the Java Algorithm emphasizes stability, adaptive enhancements, and efficacy in solving uncertain or diverse data problems. It remains an attractive choice for intricate optimization tasks across scientific and industrial domains dealing with extensive data, requiring minimal parameter adjustments, thereby asserting a significant role in the realm of optimization [23][24][25].

## C. Particle Swarm Optimization (PSO)

PSO is a nature-inspired algorithm that emulates the collective behavior observed in swarms [26]. It employs particles or agents forming a swarm to explore a search space in pursuit of the optimal solution for a given problem. Initially, random positioning of particles represents potential solutions, which are iteratively refined by the algorithm. Each particle updates its position based on both its personal experience and the best position discovered by the entire swarm. This process involves adjusting particle velocity and position using a formula that integrates personal and global best positions. Over iterations, particles traverse the search space, progressively converging toward an optimal or nearly optimal solution. The fundamental strategy involves maintaining a balance between exploration, seeking new solution areas, and exploitation, leveraging promising regions, to effectively navigate and determine the best solution. PSO's effectiveness stems from its simplicity, ease of implementation, and its ability to explore intricate search spaces, rendering it a widely adopted optimization technique across diverse domains [27][28][29].

# D. Shuffled Frog-Leaping Algorithm (SFLA)

SFLA is a metaheuristic optimization algorithm inspired by the behavior of frogs. It mimics the process of frogs hopping among lily pads to find the optimal solution for a given problem [30]. SFLA consists of a population of frogs, where each frog represents a potential solution to the optimization problem. The algorithm operates through a series of steps: initialization, grouping, memorization, shuffling, evaluation, selection and iteration. SFLA's core principle lies in the collaboration and exchange of information between frogs, resembling the way frogs leap between different lily pads to find better feeding spots. By combining local search and information sharing among frogs, SFLA aims to efficiently explore the search space and converge towards the optimal or near-optimal solutions for the given problem. Its adaptability and effectiveness in solving various optimization problems have made it a notable algorithm in the field of optimization [31][32][33].

### E. Teaching-Learning-Based Optimization (TLBO)

TLBO is a metaheuristic algorithm inspired by the teaching and learning process observed in a classroom. It simulates the learning environment where a teacher and students interact to improve learning [34]. In TLBO, the population is divided into teachers and learners. Teachers represent the best solutions, and learners are solutions that need improvement. The algorithm iteratively improves the learner's solutions based on the teacher's guidance. It consists of two phases: First, Teacher Phase: The best solutions (teachers) share their knowledge with other solutions (learners). The teaching process involves updating the learners based on the teacher's quality, allowing learners to improve towards better solutions. Second, Learner Phase: In this phase, learners assimilate knowledge from their teachers. They update their solutions by considering the information received from teachers, aiming to enhance their performance. TLBO operates by fostering collaboration and knowledge sharing among solutions to optimize the objective function. Its simplicity, ease of implementation, and ability to solve complex optimization problems make it a popular choice in various domains [35][36][37].

#### **IV. EXPERIMENTS AND RESULTS**

Our objective is to monitor CO<sub>2</sub> emissions resulting from energy consumption by seeking an accurate prediction with the lowest error. The dataset selected for this purpose pertains to Thailand and encompasses various dimensions, including GDP, population, coal and coal products, crude oil and petroleum products, gas, electricity, and CO<sub>2</sub> emissions, spanning the years from 1990 to 2020. The data was collected from the World Databank [38] and The Expert Group on Energy Data and Analysis (EGEDA)[39]. In this experiment, as mentioned earlier, the dataset was utilized to split the data into a training set and testing set, with proportions of 85% and 15%, respectively. The neural network architecture consists of three layers: 1) the input layer, 2) Hidden layer 1, starting with 5 nodes and incrementing by 5 nodes up to 20 nodes, and 3) the output layer representing carbon dioxide emissions. The hyperparameters, including the learning rate and momentum, were set to identical values, specifically 0.1. The number of iterations was fixed at 1000, and the weight values ranged from -1 to 1. The population size of all metaheuristic algorithms is 50. Various indices are typically used to evaluate and validate prediction models and algorithms. The MSE and MAE indices were used in study to validate the prediction accuracy of the six machine learning algorithms and the multiobjective mathematical model. Annual CO2 emissions target data are shown in Figure 1.



Fig. 1. Annual CO<sub>2</sub> emissions in Thailand (1990–2020)

The Pearson correlation coefficient (R) was employed to examine the dependency between each input variable and the annual output. All relevant R-values are presented in Table I.

From Table I, it is evident that the R-values for each input are close to 1, indicating a positive correlation and a direct linear relationship between the inputs and outputs.

 
 TABLE I.
 The relationships (r) between input parameters and output

| GDP    | Population | Coal<br>and coal<br>products | Crude oil<br>and<br>petroleum<br>products | Gas    | Electricity |  |
|--------|------------|------------------------------|---|--------|-------------|--|
| 0.9857 | 0.8809     | 0.8167                       | 0.9676                                    | 0.9167 | 0.9685      |  |

MSE was applied to calculate the minimize objective function performance during training as follows:

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (X_i - Y_i)^2$$

The MAE was evaluated for the reliability as follows:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |X_i - Y_i|$$

Where  $X_i$  and  $Y_i$  are actual value and predicted value, respectively; n is the number of observations.

The result from all architectures according to the MSE values obtained from the training, and the MAE from the test dataset are summarized in Table II, as follows.

TABLE II. COMPARISON OF THE MSE VALUES OBTAINED FROM TRAINING AND THE MAE VALUES OBTAINED FROM TESTING

| Algorithm | MSE from Training |        |        |        | MAE from Testing |        |        |        |
|-----------|-------------------|--------|--------|--------|------------------|--------|--------|--------|
|           | 6-5-1             | 6-10-1 | 6-15-1 | 6-20-1 | 6-5-1            | 6-10-1 | 6-15-1 | 6-20-1 |
| BPMLP     | 0.0118            | 0.0020 | 0.0017 | 0.0014 | 8.1821           | 2.6573 | 3.5633 | 3.7163 |
| BPBBO     | 0.0133            | 0.0056 | 0.0064 | 0.0088 | 0.1154           | 0.0746 | 0.0799 | 0.0940 |
| BPJAYA    | 0.0001            | 0.0389 | 0.0800 | 0.0524 | 0.2319           | 0.1972 | 0.2829 | 0.2290 |
| BPPSO     | 0.0047            | 0.0042 | 0.0046 | 0.0039 | 0.0687           | 0.0648 | 0.0676 | 0.0626 |
| BPSFLA    | 0.0076            | 0.0075 | 0.0054 | 0.0054 | 0.2162           | 0.2077 | 0.3199 | 0.3431 |
| BPTLBO    | 0.0468            | 0.0431 | 0.1023 | 0.1177 | 0.0871           | 0.0868 | 0.0732 | 0.0737 |

Table III displays the average ranks resulting from the Friedman test conducted among the six competing algorithms. Lower scores indicate better performance. The results revealed that BPMLP had a lower MSE than BPPSO when evaluated on the training dataset. However, in the case of the MAE on the testing dataset, BPMLP exhibited a higher value compared to BPPSO. This divergence may suggest a scenario of overfitting in BPMLP.

TABLE III. COMPARISON OF THE MSE VALUES OBTAINED FROM TRAINING AND THE MAE VALUES OBTAINED FROM TESTING

| Algorithm  | Ranking |      |  |  |  |
|------------|---------|------|--|--|--|
| Algorithin | MSE     | MAE  |  |  |  |
| BPMLP      | 1.75    | 6.00 |  |  |  |
| BPBBO      | 4.00    | 2.75 |  |  |  |
| BPJAYA     | 4.00    | 4.25 |  |  |  |
| BPPSO      | 2.00    | 1.00 |  |  |  |
| BPSFLA     | 6.00    | 4.75 |  |  |  |
| BPTLBO     | 3.25    | 2.25 |  |  |  |

The results indicate that BPPSO effectively determines an appropriate search agent among all the compared methods. Observing the experimental outcomes, it's evident that the MSE and MAE rank values are the lowest for BPPSO, surpassing most values obtained by BP, except for the MSE training value, which might indicate an overfitting issue. These findings demonstrate the superior performance of BPPSO in solving the problem.

Furthermore, the evaluation of the annual CO2 emissions through Table II and III reveals distinct patterns in the predictive accuracy of various algorithms. The BPPSO architecture within the artificial neural network stands out prominently, showcasing unparalleled promise in minimizing errors associated with  $CO_2$  emission predictions. Its robust performance, as indicated by the convergence curves in Figure 2, substantiates its superiority over alternative algorithms.

The MSE convergence curves depicted in Figure 2 provide a visual representation of the model's learning dynamics across different optimization techniques. It is evident from these curves that the neural network model, when trained by BBO, JAYA, PSO, SFLA, and TLBO, converges toward optimal solutions. Notably, the curve corresponding to PSO exhibits a distinct convergence pattern, underscoring the effectiveness of the PSO technique in minimizing the mean squared error.

The success of PSO in integrating solutions is evident from the convergence of the MSE curve towards the best-fit function, highlighting the algorithm's adeptness in navigating the solution space. Comparative analysis accentuates the competitive edge of PSO over other optimization algorithms utilized in this study. Its consistent and efficient convergence demonstrates superior performance, emphasizing its viability for optimizing neural network models in predicting CO<sub>2</sub> emissions.

In conclusion, the comprehensive analysis of Table II, Table III, and Figure 2 underscores the supremacy of the BPPSO architecture and the effectiveness of PSO in enhancing the accuracy of  $CO_2$  emission predictions. These findings offer valuable insights into leveraging specific neural network architectures and optimization algorithms for addressing environmental concerns associated with  $CO_2$  emissions.

# V. CONCLUSION

In this article, BPMLP was used to predict carbon dioxide emissions, employing a metaheuristic algorithm for initializing the weights of MLP. The aim of the training problem was to avoid overfitting while converging to the best possible solution. From the evaluation of various predictive models applied in conjunction with BP, namely BBO, JAYA, PSO, SFLA and TLBO, the BPPSO model exhibited the low MSE on the training dataset and the lowest MAE on the testing dataset when compared to BPMLP and other metaheuristic algorithms. BPPSO method has been proven suitable for forecasting annual carbon dioxide emissions, supporting precise energy management policies.

In future investigations, it is planned to conduct a comprehensive comparison among various metaheuristic algorithms. Furthermore, the application of neural networks in conjunction with these metaheuristic algorithms can be extended to address a diverse array of challenges beyond carbon emissions prediction. This could encompass tackling finance-related complexities, strategic planning, or solving various other problem domains. Exploring these applications could unveil the versatility and robustness of the proposed approach in handling a wide spectrum of real-world issues.



Fig. 2. Convergence curves of metaheuristic methods based on the MLP architecture during training for MSE

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#### REFERENCES

- J. Houghton, "Global warming," *Reports Prog. Phys.*, vol. 68, no. 6, p. 1343, 2005.
- [2] M. E. Javanmard, Y. Tang, Z. Wang, and P. Tontiwachwuthikul, "Forecast energy demand, CO2 emissions and energy resource

impacts for the transportation sector," *Appl. Energy*, vol. 338, p. 120830, 2023.

- [3] H.-T. Pao and C.-M. Tsai, "Modeling and forecasting the CO2 emissions, energy consumption, and economic growth in Brazil," *Energy*, vol. 36, no. 5, pp. 2450–2458, 2011.
- [4] S. M. Hosseini, A. Saifoddin, R. Shirmohammadi, and A. Aslani, "Forecasting of CO2 emissions in Iran based on time series and regression analysis," *Energy Reports*, vol. 5, pp. 619–631, 2019.
- [5] T. Hong, K. Jeong, and C. Koo, "An optimized gene expression programming model for forecasting the national CO2 emissions in 2030 using the metaheuristic algorithms," *Appl. Energy*, vol. 228, pp. 808–820, 2018.
- [6] Ü. Ağbulut, "Forecasting of transportation-related energy demand and

CO2 emissions in Turkey with different machine learning algorithms," *Sustain. Prod. Consum.*, vol. 29, pp. 141–157, 2022.

- [7] L. Wen and X. Yuan, "Forecasting CO2 emissions in Chinas commercial department, through BP neural network based on random forest and PSO," *Sci. Total Environ.*, vol. 718, p. 137194, 2020.
- [8] A. Sangeetha and T. Amudha, "A novel bio-inspired framework for CO2 emission forecast in India," *Procedia Comput. Sci.*, vol. 125, pp. 367–375, 2018.
- [9] R. Kruse, S. Mostaghim, C. Borgelt, C. Braune, and M. Steinbrecher, "Multi-layer perceptrons," in *Computational intelligence: a methodological introduction*, Springer, 2022, pp. 53–124.
- [10] R. Hecht-Nielsen, "Theory of the backpropagation neural network," in *Neural networks for perception*, Elsevier, 1992, pp. 65–93.
- [11] S. P. Siregar and A. Wanto, "Analysis of artificial neural network accuracy using backpropagation algorithm in predicting process (forecasting)," *IJISTECH (International J. Inf. Syst. Technol.*, vol. 1, no. 1, pp. 34–42, 2017.
- [12] A. Sharaff and S. R. Roy, "Comparative analysis of temperature prediction using regression methods and back propagation neural network," in 2018 2nd international conference on trends in electronics and informatics (ICOEI), 2018, pp. 739–742.
- [13] W. Sun and C. Huang, "A carbon price prediction model based on secondary decomposition algorithm and optimized back propagation neural network," *J. Clean. Prod.*, vol. 243, p. 118671, 2020.
- [14] X.-S. Yang, Nature-inspired metaheuristic algorithms. Luniver press, 2010.
- [15] A. H. Gandomi, X.-S. Yang, S. Talatahari, and A. H. Alavi, "Metaheuristic algorithms in modeling and optimization," *Metaheuristic Appl. Struct. infrastructures*, vol. 1, pp. 1–24, 2013.
- [16] T. Dokeroglu, E. Sevinc, T. Kucukyilmaz, and A. Cosar, "A survey on new generation metaheuristic algorithms," *Comput. Ind. Eng.*, vol. 137, p. 106040, 2019.
- [17] X.-S. Yang, "Metaheuristic optimization: algorithm analysis and open problems," in *International symposium on experimental algorithms*, 2011, pp. 21–32.
- [18] D. Simon, "Biogeography-based optimization," *IEEE Trans. Evol. Comput.*, vol. 12, no. 6, pp. 702–713, 2008, doi: 10.1109/TEVC.2008.919004.
- [19] S. Mirjalili, S. M. Mirjalili, and A. Lewis, "Let a biogeography-based optimizer train your multi-layer perceptron," *Inf. Sci. (Ny).*, vol. 269, pp. 188–209, 2014.
  [20] H. Ma, D. Simon, P. Siarry, Z. Yang, and M. Fei, "Biogeography-
- [20] H. Ma, D. Simon, P. Siarry, Z. Yang, and M. Fei, "Biogeographybased optimization: a 10-year review," *IEEE Trans. Emerg. Top. Comput. Intell.*, vol. 1, no. 5, pp. 391–407, 2017.
- [21] B. T. Pham, M. D. Nguyen, K. T. T. Bui, I. Prakash, K. Chapi, and D. T. Bui, "A novel artificial intelligence approach based on Multi-layer Perceptron Neural Network and Biogeography-based Optimization for predicting coefficient of consolidation of soil," *Catena*, vol. 173, pp. 302–311, Feb. 2019, doi: 10.1016/j.catena.2018.10.004.
- [22] R. Venkata Rao, "Jaya: A simple and new optimization algorithm for solving constrained and unconstrained optimization problems," *Int. J. Ind. Eng. Comput.*, vol. 7, no. 1, pp. 19–34, 2016, doi: 10.5267/j.ijiec.2015.8.004.
- [23] E. Uzlu, "Application of Jaya algorithm-trained artificial neural networks for prediction of energy use in the nation of Turkey," *Energy Sources, Part B Econ. Planning, Policy*, vol. 14, no. 5, pp. 183–200, 2019.
- [24] P. Singh, K. K. Mishra, and P. Dwivedi, "Enhanced hybrid model for

electricity load forecast through artificial neural network and Jaya algorithm," in 2017 International conference on intelligent computing and control systems (ICICCS), 2017, pp. 115–120.

- [25] N. Setyawan, M. Nasar, and N. Mardiyah, "Jaya-neural network for server room temperature forecasting through sensor network," in 2019 International Electronics Symposium (IES), 2019, pp. 428–431.
- [26] J. Kennedy and R. Eberhart, "Particle swarm optimization," in Proceedings of ICNN'95-international conference on neural networks, 1995, vol. 4, pp. 1942–1948.
- [27] M. Carvalho and T. B. Ludermir, "Particle swarm optimization of neural network architectures andweights," in 7th International Conference on Hybrid Intelligent Systems (HIS 2007), 2007, pp. 336– 339.
- [28] A. Roy, D. Dutta, and K. Choudhury, "Training artificial neural network using particle swarm optimization algorithm," *Int. J. Adv. Res. Comput. Sci. Softw. Eng.*, vol. 3, no. 3, 2013.
- [29] J. Aguila-Leon, C. Vargas-Salgado, C. Chiñas-Palacios, and D. Díaz-Bello, "Energy management model for a standalone hybrid microgrid through a particle Swarm optimization and artificial neural networks approach," *Energy Convers. Manag.*, vol. 267, p. 115920, 2022.
- [30] M. Eusuff, K. Lansey, and F. Pasha, "Shuffled frog-leaping algorithm: a memetic meta-heuristic for discrete optimization," *Eng. Optim.*, vol. 38, no. 2, pp. 129–154, 2006.
- [31] S. Debata, C. K. Samanta, and S. P. Panigrahi, "Efficient energy management strategies for hybrid electric vehicles using shuffled frog-leaping algorithm," *Int. J. Sustain. Eng.*, vol. 8, no. 2, pp. 138– 144, 2015.
- [32] R. K. Kumar and S. V. A. Rao, "Neural Network with Hybrid Shuffled Frog," *framework*, vol. 14, no. 5, 2016.
- [33] F. U. Xiaomin, "Short-Term Wind Speed Prediction Based on Improved Wavelet Transform and Shuffled Frog Leaping Difference Evolution Neural Network Algorithm," *Distrib. Energy Resour.*, vol. 6, no. 6, pp. 38–44, 2022.
- [34] R. V. Rao, V. J. Savsani, and D. P. Vakharia, "Teaching-learningbased optimization: A novel method for constrained mechanical design optimization problems," *CAD Comput. Aided Des.*, vol. 43, no. 3, pp. 303–315, Mar. 2011, doi: 10.1016/j.cad.2010.12.015.
- [35] E. Uzlu, M. Kankal, A. Akpınar, and T. Dede, "Estimates of energy consumption in Turkey using neural networks with the teaching– learning-based optimization algorithm," *Energy*, vol. 75, pp. 295– 303, 2014.
- [36] M. Kankal and E. Uzlu, "Neural network approach with teaching– learning-based optimization for modeling and forecasting long-term electric energy demand in Turkey," *Neural Comput. Appl.*, vol. 28, no. 1, pp. 737–747, 2017.
- [37] K. Li, X. Xie, W. Xue, X. Dai, X. Chen, and X. Yang, "A hybrid teaching-learning artificial neural network for building electrical energy consumption prediction," *Energy Build.*, vol. 174, pp. 323– 334, 2018.
- [38] The World Bank, "World Development Indicators." https://databank.worldbank.org/source/world-developmentindicators
- [39] Expert Group on Energy Data and Analysis (EGEDA), "the APEC Energy Database." https://www.egeda.ewg.apec.org/egeda/database info/index.html